



# AUTONOMOUS SKILL ACQUISITION IN REINFORCEMENT LEARNING USING LOCALITY BASED GRAPH THEORETIC FEATURES

Semiha Hazel Çavuş  
semihazel@gmail.com

Zeynep Kumralbaş  
zeynepkumralbas@gmail.com

Advisor: Assoc. Prof. Borahan Tümer

## Abstract

In this project, we aim to reduce the time complexity of subgoal detection in Hierarchical Reinforcement Learning (HRL).

**Problem:** There are different approaches for detecting subgoals. Betweenness Centrality a graph based approach, is one of the well performed techniques. Since the time complexity for subgoal detection is  $O(n^3)$  for each episode, it brings a computational burden.

**Solution:** Dynamic Community Detection algorithm which runs in  $O(|\Delta E| \cdot |E| + |E|^2)$  can be used for subregion detection. Hence, subgoals are detected using these subregions.

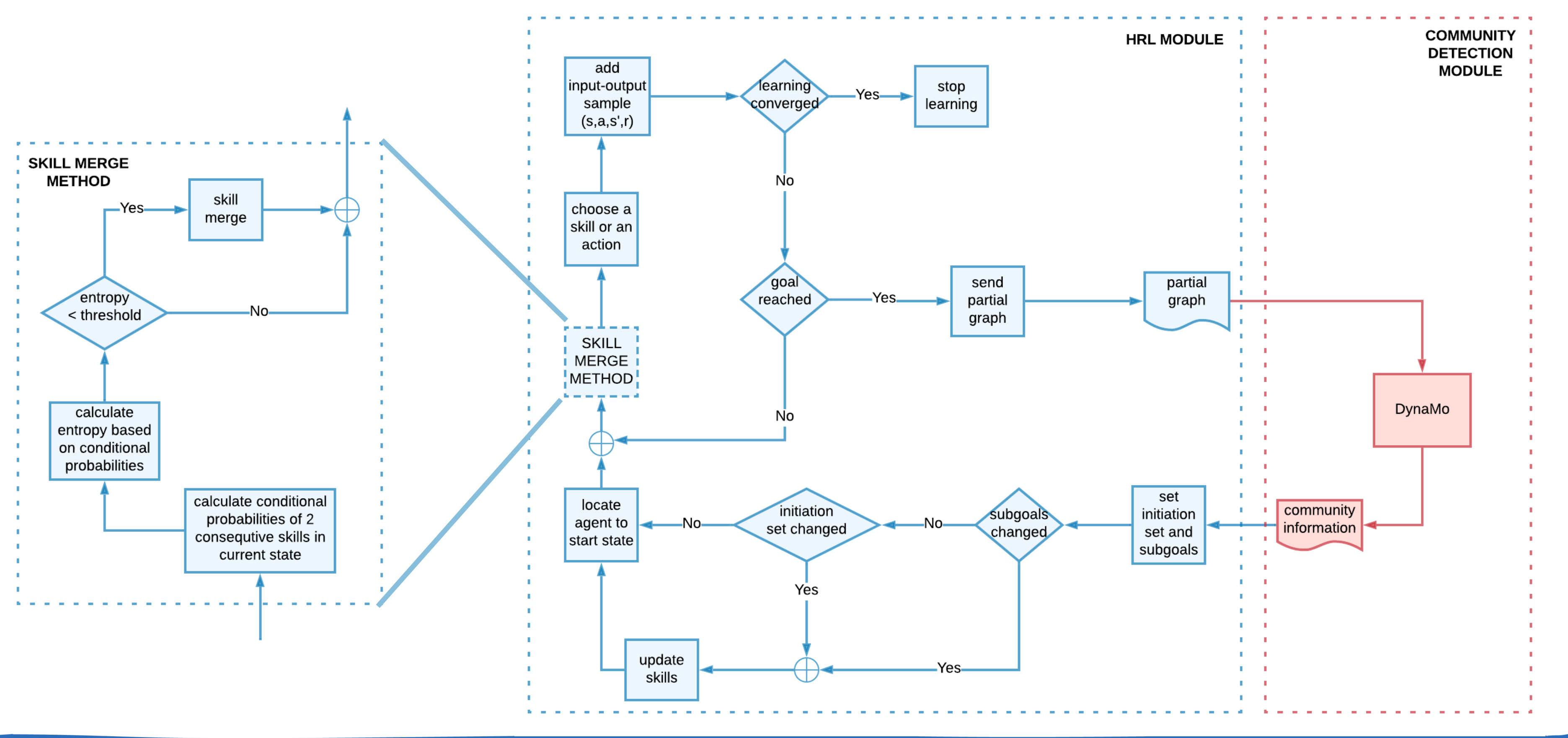
### Problem of Community Detection:

- It can further partition a subregion (over-segmentation),
- It can combine two or more subregions as one subregion (under-segmentation).

### Solution:

- Since subgoals are detected to construct options, option merging can solve this over-segmentation.
- Under-segmentation is mostly solvable by adjusting the parameters.

## Flow Chart



## Reinforcement Learning (RL)

RL is a machine learning technique where an agent takes an action in an environment, moves to the next state and receives rewards or punishments regarding this new state.

So, it can learn a satisfactory (hopefully optimal or possibly a near optimal) policy that leads the agent to the goal state in the environment.

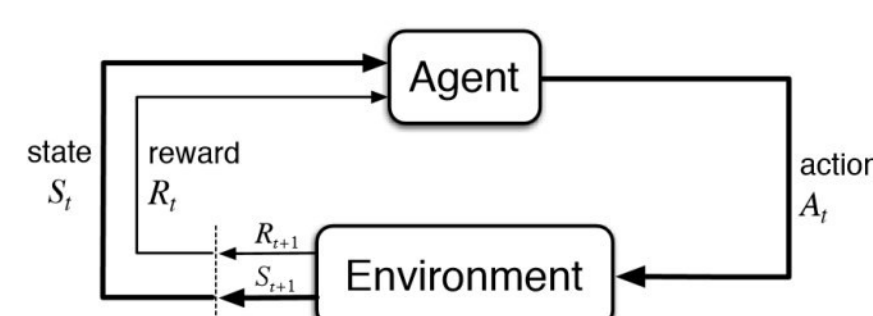


Fig. 1: RL diagram

## Hierarchical Reinforcement Learning (HRL)

As the environment grows too large, converging to a satisfactory policy for regular RL algorithms such as flat Q-learning becomes quickly infeasible.

In HRL:

- Environment is split into subregions.
- A subpolicy (sequence of primitive actions) is learned for each subregion.
- The sequence of primitive actions is called skill/option.

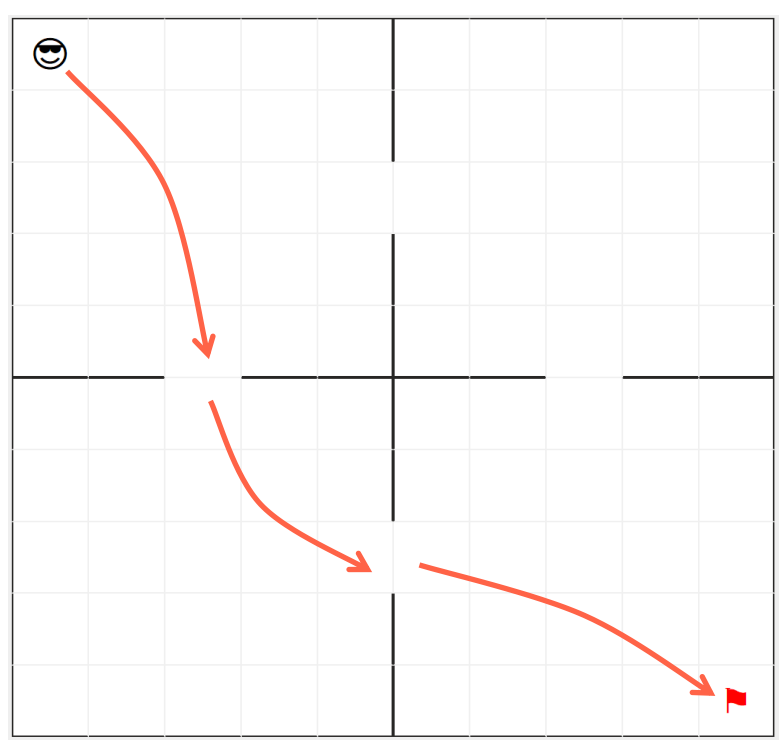


Fig. 2: Skills in HRL

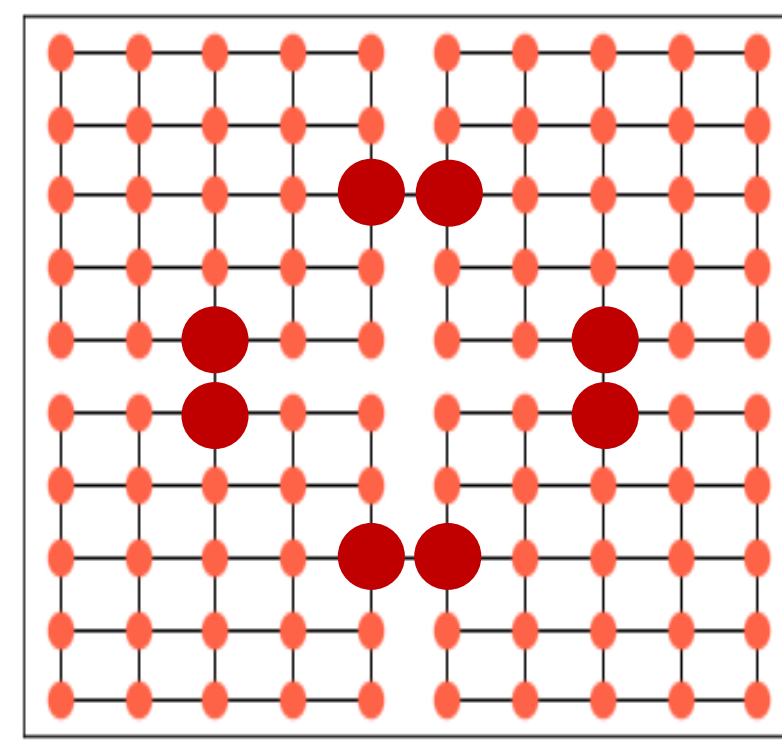


Fig. 3: Subgoals on graph representation of Fig. 2

An option consists of three components:

- A policy  $\pi: S \times A \rightarrow [0,1]$
- An initiation set  $I \subseteq S$
- A termination condition  $\beta: S \rightarrow [0,1]$

## Time Complexity

**Betweenness Centrality:**  $g(v) = \sum_{s \neq v \neq t} \frac{\sigma_{st}(v)}{\sigma_{st}}$   $\sigma_{st}$ : total number of shortest paths from node  $s$  to node  $t$   $\sigma_{st}(v)$ : number of those paths that pass through  $v$  Average case:  $O(|V|^3)$

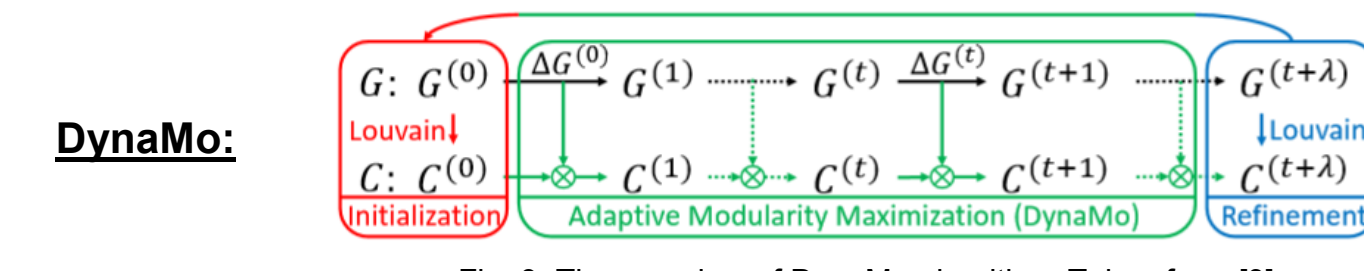


Fig. 9: The overview of DynaMo algorithm. Taken from [3]

$C$ : a set of communities associated with  $G$   
 $G$ : a sequence of graph snapshots

### Best Case:

$$O(|\Delta E| + |E|^2)$$

$|E|$ : total number of edges

$|V|$ : total number of nodes

$|\Delta E|$ : number of added/removed edges

$|E|'$ : the number of edges evaluated in the second phase of the algorithm

$|E|' \ll |E|$

### Worst Case:

$$O(|\Delta E| \cdot |E| + |E|^2)$$

## Experimental Results

We have done approximately 30 experiments on different types of environments and get similar results. The figures below are the representative ones.

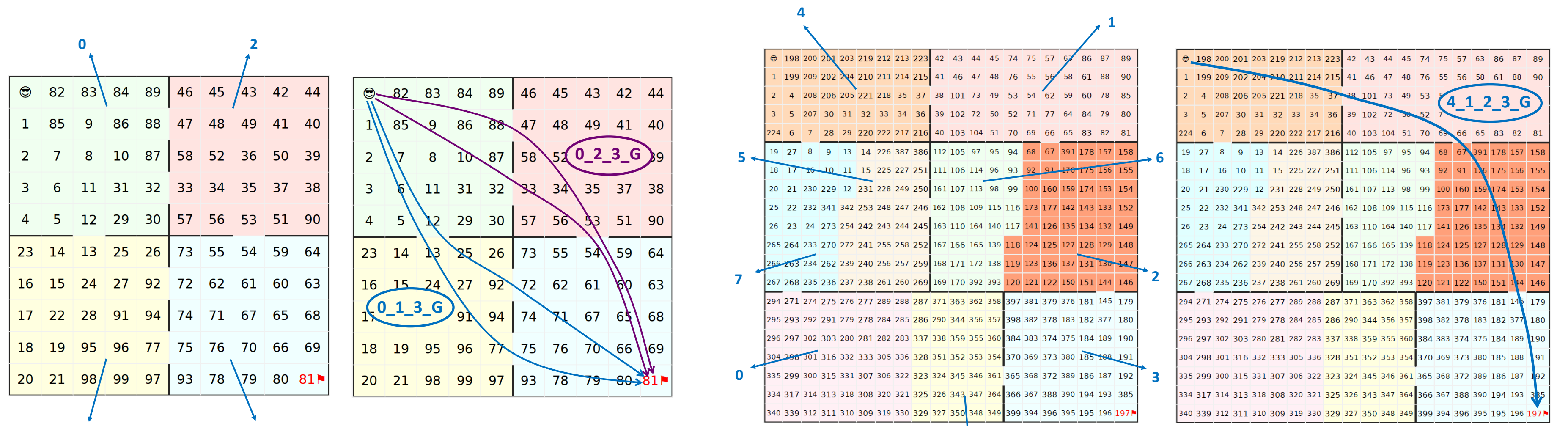


Fig. 10: Communities of 10x10 environment

Fig. 11: Merged options

Fig. 12: Communities of 20x20 environment

Fig. 13: Merged options

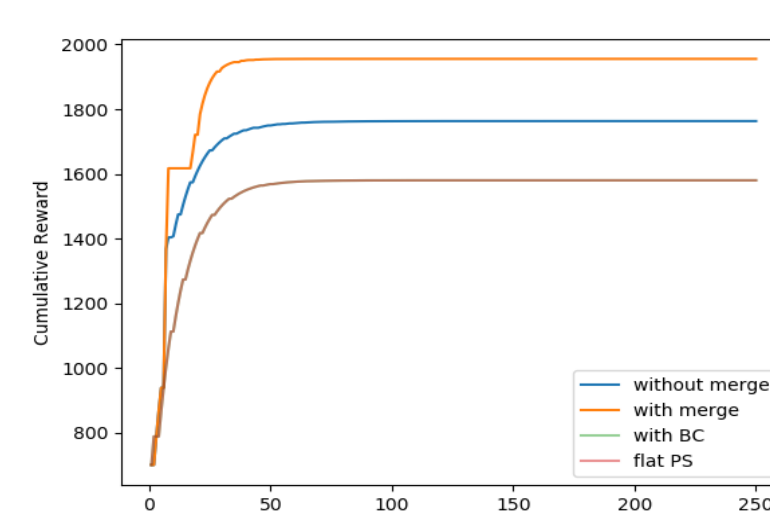


Fig. 14: Cumulative reward graph

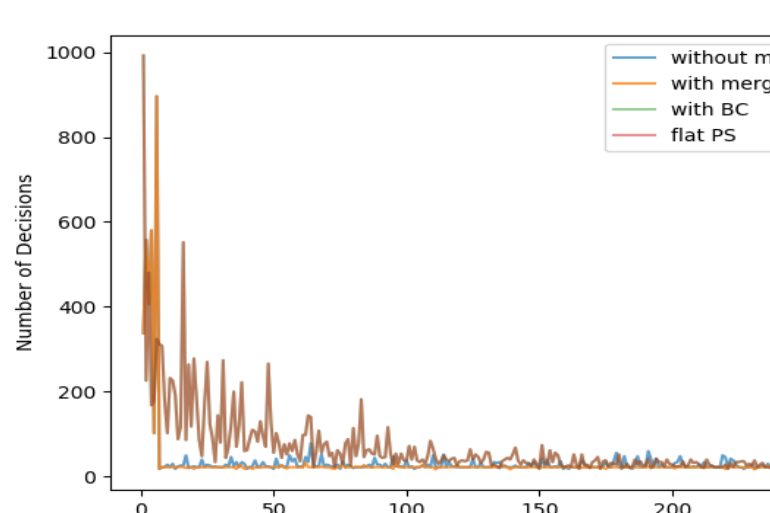


Fig. 15: Number of decisions graph

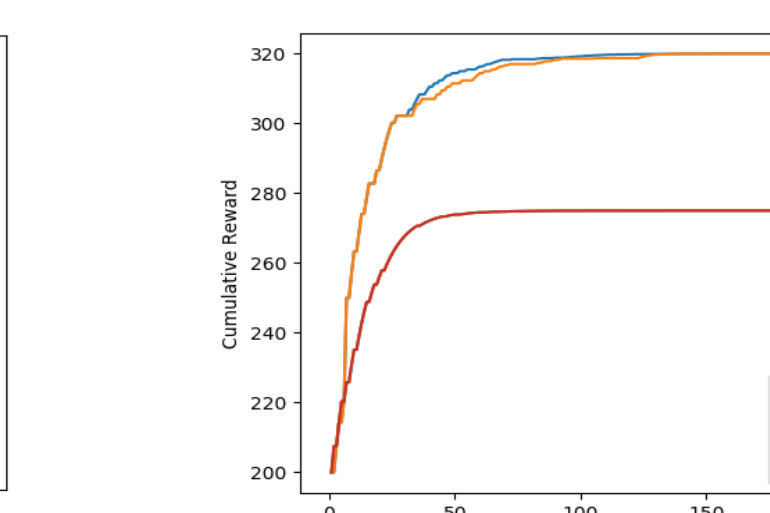


Fig. 16: Cumulative reward graph

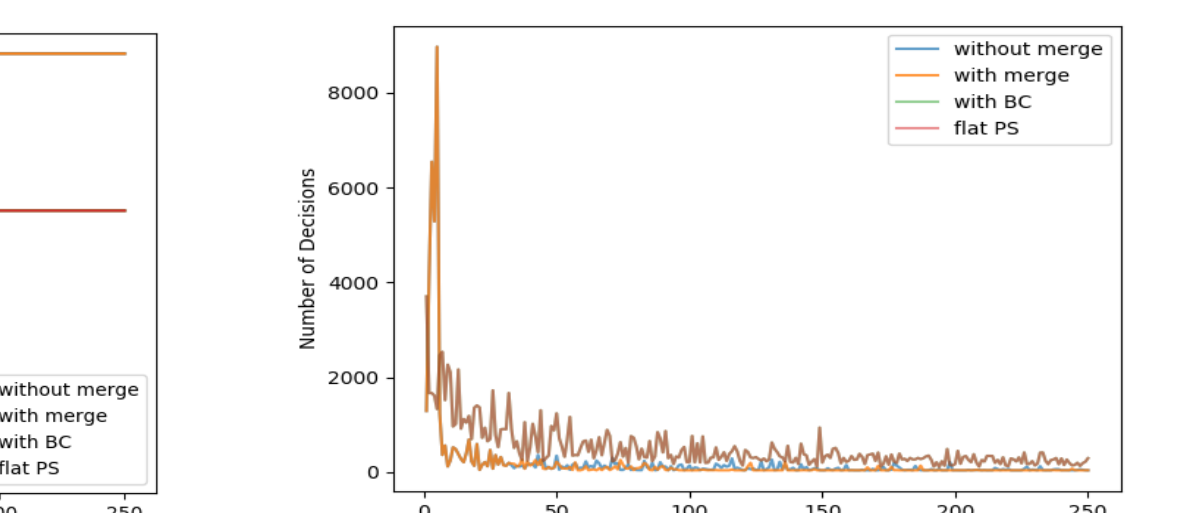


Fig. 17: Number of decisions graph

## Community Detection

Community Detection algorithms try to maximize the modularity which is used as an objective function.

**Modularity:** A metric that represents how strongly nodes are connected to each other in each community.

$$Q = \frac{1}{2m} \sum_{i,j} [A_{ij} - \gamma \frac{k_i k_j}{2m}] \delta(c_i, c_j)$$

$A_{ij}$ : the number of the edges between nodes  $i$  and  $j$   
 $k_i$ : the degree of node  $i$ ,  $k_j$ : the degree of node  $j$   
 $\delta(c_i, c_j)$ : 1 if nodes  $i$  and  $j$  belong to same community, 0 otherwise  
 $m$ : total number of edges in the network  
 $\gamma$ : resolution parameter

**DynaMo:** A dynamic community detection algorithm which updates communities locally.

Partial graphs change in time  $\rightarrow$  A dynamic approach  
 DynaMo

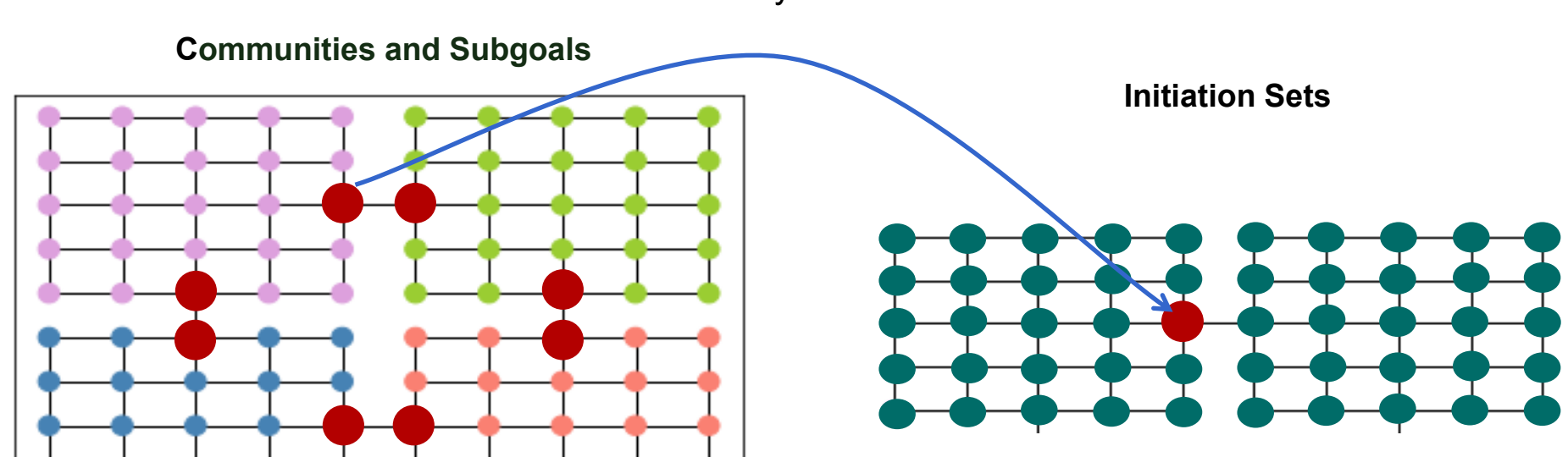


Fig. 4: Subgoals on accurately detected communities

Fig. 5: Initiation set of the shown subgoal

Communities may not be found correctly, since resolution parameter which changes the size of the communities is not set adaptively according to the structure of the graph.

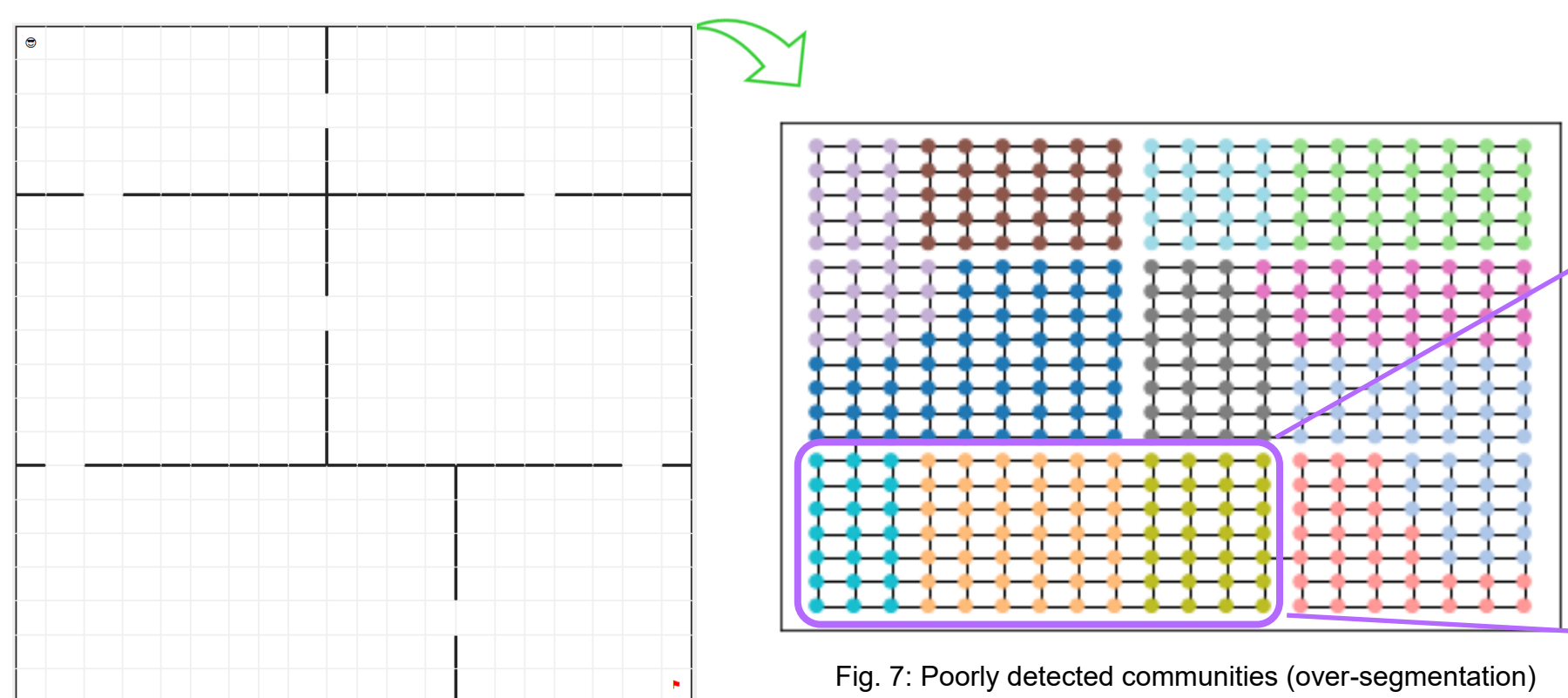


Fig. 6: 20x20 environment

Fig. 7: Poorly detected communities (over-segmentation)

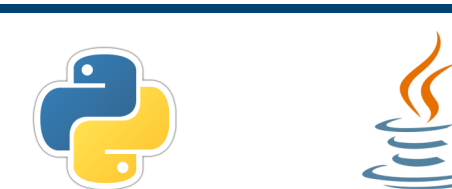
Fig. 8: Examples of community borders

## Conclusion

- Autonomous skill acquisition is achieved.
- Skill merge approach converges faster.
- Setting resolution parameter adaptively.
- Complexity of subgoal detection is improved.
- The number of decisions agent has to take is decreased.
- Finding more robust function to select probabilities of skills to be merged.

## Future Work

### Technologies Used



### Acknowledgement

We would like to thank Kutalmış Coşkun for his precious contributions to Project.

### Selected References

- [1] Sutton, Richard S., Doina Precup, and Satinder Singh. "Between MDPs and semi-MDPs: A framework for temporal abstraction in reinforcement learning." Artificial intelligence 112.1-2 (1999): 181-211.
- [2] Şimşek, Özgür, and Andrew G. Barto. "Skill characterization based on betweenness." Advances in neural information processing systems. 2009.
- [3] ZHUANG, DI, CHANG, J., MORRIS, LI, MINGCHEN. DynaMo: Dynamic Modularity-based Community Detection in Evolving Social Networks. arXiv preprint arXiv:1709.08350, 2017.